# An ab Initio Study of the Vibrational Spectrum of Bicyclo[1.1.0]but-1(3)-ene 

B. Andes Hess, Jr., ${ }^{+\dagger}$ Wesley D. Allen, ${ }^{\ddagger, \delta}$ D. Michalska, ${ }^{\dagger, \perp}$ L. J. Schaad, ${ }^{*+}$ and Henry F. Schaefer, III* ${ }^{*}$<br>Contribution from the Departments of Chemistry, Vanderbilt University, Nashville, Tennessee 37235, and University of California, Berkeley, California 94720. Received August 8, 1986


#### Abstract

Vibrational force constants, frequencies, and IR intensities calculated with several basis sets at the SCF level and with inclusion of electron correlation are reported for bicyclo[1.1.0]but-1(3)-ene. Bicyclobutene (5) is predicted to have a singlet ground state with a nonplanar carbon skeleton. Its IR spectrum should consist of two absorptions in the C-H stretch region, a series of weak bands between 600 and $1800 \mathrm{~cm}^{-1}$, and at lower frequencies a very intense and a quite weak absorption. Its computed energy relative to other known $\mathrm{C}_{4} \mathrm{H}_{4}$ isomers suggests that it will be stable only at very low temperatures in a matrix. The barrier to ring inversion is predicted to be $12 \mathrm{kcal} / \mathrm{mol}$. Finally, geometrical structures, adiabatic and vertical excitation energies, and vibrational frequencies are reported for the lowest triplet state ( ${ }^{3} \mathrm{~B}_{1}$ ) of bicyclobutene (5).


The continued theoretical and synthetic interest in unusual molecules on the $\mathrm{C}_{4} \mathrm{H}_{4}$ potential surface [e.g., methylenecyclopropene (1), ${ }^{1-5}$ tetrahedrane (2),,$^{6-9}$ cyclobutadiene (3), ${ }^{10-20}$ and

1

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cyclobutyne (4) ${ }^{21}$ ] has led us to carry out an ab initio theoretical vibrational analysis of bicyclo[1.1.0]but-1(3)-ene (5). Both


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cyclobutadiene and methylenecyclopropene have been prepared, but tetrahedrane, cyclobutyne, and bicyclobutene are as yet unknown, although Szeimies has shown that three tricyclic bicyclobutene derivatives $(6-8)$ may exist as transient species. ${ }^{22}$ For

the two known systems (1 and 3) computed ab initio IR spectra played an important role in the confirmation of their synthesis. Cyclobutadiene was initially reported ${ }^{11.12}$ to have a square structure, but later ${ }^{13.16-19}$ observed and computed IR spectra showed it to be a rectangular molecule. The synthesis of methylenecyclopropene was also in part confirmed by the computation of its IR spectrum. ${ }^{1,4,5}$ We have recently reported the computed vibrational spectra of tetrahedrane ${ }^{6}$ and cyclobutyne ${ }^{21}$ in order that these spectra might be useful in their eventual identification. Similarly we report here the vibrational spectrum of bicyclo-[1.1.0]but-1 (3)-ene (5).

Hehre and Pople ${ }^{23}$ reported the first calculation on 5 in 1975 with the STO-3G basis set, and surprisingly it was predicted to have a nonplanar carbon skeleton ( $C_{2 v}$ ) with the double bond carbons significantly pyramidalized. More recent theoretical studies on highly strained cycloalkenes have shown that pyramidalization of double bond carbons is likely to be a common phenomenon in such systems. ${ }^{24}$ On the basis of model calculations on ethylene, Schleyer, Pople, and co-workers ${ }^{25}$ have suggested that when the $\mathrm{R}-\mathrm{C}=\mathrm{C}$ angle is constrained to be less than $100^{\circ}$,

[^0]pyramidalization of the double bond carbons should occur. In contrast to these $a b$ initio results, Dewar ${ }^{26}$ found that a MINDO/3
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Table I. Optimized Geometry of Bicyclobutene ${ }^{a}$

| parameter ${ }^{\text {b }}$ | basis set |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | MINDO/3 ${ }^{\text {c }}$ | STO-3G ${ }^{\text {d.e }}$ | $4-31 \mathrm{G}^{\text {ef }}$ | $6.31 \mathrm{G}^{* 8}$ | $\begin{gathered} \text { MP2 } \\ 6-31 G^{* g} \end{gathered}$ | $\begin{aligned} & \text { TCSCF } \\ & 6-31 G^{* g} \end{aligned}$ | $\begin{gathered} \hline \text { TCSCF } \\ \text { DZP }^{8} \end{gathered}$ | $\begin{aligned} & \text { 2R CISD } \\ & 6-31 G^{* g} \end{aligned}$ |
| $R$ | 1.46 | 1.535 | 1.505 | 1.481 | 1.489 | 1.479 | 1.487 | 1.483 |
| $S$ | 1.53 | 1.343 | 1.353 | 1.344 | 1.412 | 1.375 | 1.383 | 1.385 |
| $T$ | 1.12 | 1.086 | 1.068 | 1.073 | 1.086 | 1.074 | 1.077 | 1.081 |
| $U$ | 1.12 | 1.092 | 1.077 | 1.084 | 1.096 | 1.083 | 1.086 | 1.091 |
| $\alpha$ |  | 117.7 | 117.6 | 118.0 | 118.2 | 118.5 | 118.1 | 118.4 |
| $\beta$ |  | 128.7 | 127.6 | 127.8 | 127.6 | 127.4 | 127.3 | 127.5 |
| $\tau$ | 180.0 | 128.3 | 132.4 | 135.2 | 138.1 | 133.5 | 133.2 | 134.9 |
| energy |  | -151.65018 | -153.30584 | $-153.58020^{h}$ | -154.10804 | -153.62050 | - 153.64546 | -154.07006 |

[^1]

Figure 1. Definition of internal coordinates of bicyclobutene (5).
calculation predicts a planar carbon skeleton for 5. However, ab initio calculations with larger basis sets (4-31G and 6-31G*) ${ }^{246.25}$ have confirmed the prediction of the earlier ab initio work that the double bond carbons in 5 should be significantly pyramidalized. The computed ab initio IR spectrum should therefore be of use not only in helping to identify 5 but also in confirming its geometry, since planar and puckered carbon skeletons would be expected to yield very different IR spectra.

## Computational Methods

SCF. The (RHF) SCF calculations were performed with gaussian $80^{27}$ with use of the internally stored $6.31 \mathrm{G}^{*}$ basis set. Beginning with the optimized geometry (Figure 1 and Table I), each symmetry adapted internal coordinate in Table II was distorted by $0.01 \AA$ for bond lengths and $3^{\circ}$ for angles. Plus and minus distortions were done for coordinates of $\mathrm{A}_{1}$ symmetry and single distortions for the remainder. The Cartesian coordinates of these distorted structures were obtained with use of the BMAT link of Pulay's program texas. ${ }^{28,29}$ From these coordinates gaUSSIAN 80 input was computed, and the analytic gradient and dipole moment were calculated and transformed to the original Cartesian coordinates generated by bmat. The Cartesian gradient for each structure was converted to forces with respect to each internal symmetry coordinate. After computation of the force constants (Table III) from these internal forces, a standard Wilson GF analysis gave vibrational frequencies (Table IV) and their normal modes. Intensities of the $A_{1}, B_{1}$, and $B_{2}$ blocks were obtained from dipole moment derivatives and the normal mode eigenvectors. ${ }^{30}$ SCF frequencies were obtained analytically with the program GAUSSIAN $82^{31}$ with the STO-3G, 4-31G, and, as a check of the above numerical frequencies, $6-31 \mathrm{G}^{*}$ basis sets.

MP2. The geometry of $\mathbf{5}$ was reoptimized (Table I) with the $6-31 \mathrm{G}^{*}$ basis set with the inclusion of electron correlation (RHF MP2). ${ }^{32}$ The carbon 1 s orbitals were frozen. For evaluation of

[^2]Table II. Symmetry Coordinates for Bicyclobutene ${ }^{a}$

| species | coordinate |
| :---: | :--- |
| $\mathrm{A}_{1}$ | $S_{1}=1 / 2\left(R_{1}+R_{2}+R_{3}+R_{4}\right)$ |
|  | $S_{2}=(2)^{-1 / 2}\left(T_{1}+T_{2}\right)$ |
|  | $S_{3}=(2)^{-1 / 2}\left(U_{1}+U_{2}\right)$ |
|  | $S_{4}=S$ |
|  | $S_{5}=1 / 2\left(\phi_{1}+\phi_{2}+\phi_{3}+\phi_{4}\right)$ |
|  | $S_{6}=1 / 2\left(\gamma_{1}+\gamma_{2}+\gamma_{3}+\gamma_{4}\right)$ |
| $\mathrm{A}_{2}$ | $S_{7}=\tau$ |
|  | $S_{8}=1 / 2\left(R_{1}-R_{2}-R_{3}+R_{4}\right)$ |
|  | $S_{10}=1 / 2\left(\phi_{1}-\phi_{2}-\phi_{3}+\phi_{4}\right)$ |
|  | $S_{11}=1 / 2\left(\gamma_{1}-\gamma_{2}-\gamma_{3}+R_{2}+R_{3}-R_{4}\right)$ |
|  | $S_{12}=1 / 2\left(\phi_{1}-\phi_{2}+\phi_{3}-\phi_{4}\right)$ |
|  | $S_{13}=1 / 2\left(\gamma_{1}-\gamma_{2}+\gamma_{3}-\gamma_{4}\right)$ |
|  | $S_{14}=1 / 2\left(R_{1}+R_{2}-R_{3}-R_{4}\right)$ |
|  | $S_{15}=(2)^{-1 / 2}\left(T_{1}-T_{2}\right)$ |
|  | $S_{16}=(2)^{-1 / 2}\left(U_{1}-U_{2}\right)$ |
|  | $S_{17}=1 / 2\left(\phi_{1}+\phi_{2}-\phi_{3}-\phi_{4}\right)$ |
|  | $S_{18}=1 / 2\left(\gamma_{1}+\gamma_{2}-\gamma_{3}-\gamma_{4}\right)$ |

${ }^{a}$ The symmetry species referred to in this paper correspond to the $C_{2 v}$ and $D_{2 h}$ character tables in ref 43 assuming the $C_{2}$ and $z$ axes are coincident and the $x$ axis lies along the $C-C$ double bond.
the MP2 force constants (Table III), the second derivatives of the energy were computed numerically. Plus and minus distortions were made for the diagonal force constants and appropriate combination distortions for the off-diagonal force constants. Diagonalization of this force constant matrix in a GF analysis gave MP2 frequencies (Table IV). No MP2 intensities were computed.

TCSCF. With use of methods developed at Berkeley, ${ }^{216}$ twoconfiguration SCF (TCSCF) computations were performed with two basis sets ( $6-31 \mathrm{G}^{*}$ and $D Z \mathrm{P}^{33}$ ) for bicyclobutene (5). A single-reference CISD ( $6-31 \mathrm{G}^{*}$ ) calculation at the optimum 6 $31 \mathrm{G}^{*}$ geometry (with carbon 1 s orbitals frozen) gave $E$ (CISD) $=-154.05192$ hartree with $C_{1}=0.928, C_{2}=-0.082$, and $C_{3}=$ 0.034 . The relatively large value of $C_{2}$ suggests that 5 might possess significant diradical character, and as a consequence a single-reference wave function might be inadequate. The TCSCF method was then used $\left(\Psi=C_{1}\right.$ det $\left|(\operatorname{core})\left(4 \mathrm{~b}_{2}\right)^{2}\left(1 \mathrm{a}_{2}\right)^{2}\left(6 \mathrm{a}_{1}\right)^{2}\left(7 \mathrm{a}_{1}\right)^{2}\right|$ $+C_{2} \operatorname{det} \mid($ core $\left.)\left(4 \mathrm{~b}_{2}\right)^{2}\left(1 \mathrm{a}_{2}\right)^{2}\left(6 \mathrm{a}_{1}\right)^{2}\left(3 \mathrm{~b}_{1}\right)^{2} \mid\right)$ with the $6-31 \mathrm{G}^{*}$ basis set to optimize the geometry (Table I) and to obtain frequencies and intensities (Table IV) with analytic second derivatives. At the optimal geometry the TCSCF coefficients were $C_{1}=0.957$ and $C_{2}=-0.290$. The geometry of 5 was also optimized with the DZP basis ( $C_{1}=0.958$ and $C_{2}=-0.288$ ) and frequencies and intensities computed. The large values of the TCSCF coefficients $C_{2}$ confirm the likely diradical character of 5 .

The optimal planar bicyclobutene structure ( $D_{2 h}$ ) was obtained with the $6-31 \mathrm{G}^{*}$ basis set. The optimized parameters found for

[^3]Table III. Calculated Force Constants for Bicyclobutene ${ }^{a}$

| species | constants | 6-31G* | $\begin{gathered} \hline 6-31 G^{*} \\ \text { MP2 } \end{gathered}$ | $\begin{gathered} \text { DZP } \\ \mathrm{TCSCF} \end{gathered}$ | $\begin{gathered} \text { 6-31G* } \\ \text { 2R CISD } \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{A}_{1}$ | $F_{11}$ | 5.276 | 5.120 | 5.375 | 5.283 |
|  | $F_{22}$ | 6.316 | 5.783 | 6.221 | 5.998 |
|  | $F_{33}$ | 5.842 | 5.398 | 5.82 .9 | 5.599 |
|  | $F_{44}$ | 8.592 | 5.337 | 6.841 | 6.617 |
|  | $F_{55}$ | 0.872 | 0.830 | 0.849 | 0.832 |
|  | $F_{66}$ | 0.857 | 0.810 | 0.828 | 0.808 |
|  | $F_{77}$ | 0.994 | 0.763 | 1.059 | 0.925 |
|  | $F_{12}$ | 0.178 | 0.152 | 0.151 | 0.165 |
|  | $F_{13}$ | 0.291 | 0.254 | 0.253 | 0.265 |
|  | $F_{14}$ | -1.041 | -0.832 | -0.892 | -0.879 |
|  | $F_{15}$ | 0.348 | 0.344 | 0.308 | 0.319 |
|  | $F_{16}$ | 0.080 | 0.089 | 0.081 | 0.083 |
|  | $F_{17}$ | -0.607 | -0.525 | -0.534 | -0.546 |
|  | $F_{23}$ | 0.065 | 0.042 | 0.051 | 0.057 |
|  | $F_{24}$ | -0.158 | -0.188 | -0.168 | -0.177 |
|  | $F_{25}$ | -0.048 | -0.049 | -0.029 | -0.035 |
|  | $F_{26}$ | -0.121 | -0.128 | -0.122 | -0.126 |
|  | $F_{27}$ | -0.012 | 0.000 | -0.031 | -0.019 |
|  | $F_{34}$ | -0.279 | -0.223 | -0.192 | -0.215 |
|  | $F_{35}$ | -0.127 | -0.126 | -0.124 | -0.124 |
|  | $F_{36}$ | -0.020 | -0.034 | -0.027 | -0.024 |
|  | $F_{37}$ | 0.037 | 0.021 | 0.026 | 0.031 |
|  | $F_{45}$ | -0.015 | -0.037 | -0.046 | -0.029 |
|  | $F_{46}$ | 0.067 | 0.135 | 0.126 | 0.120 |
|  | $F_{47}$ | 0.555 | 0.612 | 0.620 | 0.574 |
|  | $F_{56}$ | 0.387 | 0.369 | 0.378 | 0.369 |
|  | $F_{57}$ | -0.064 | -0.041 | -0.097 | -0.070 |
|  | $F_{67}$ | 0.072 | 0.052 | 0.077 | 0.073 |
| $\mathrm{A}_{2}$ | $F_{88}$ | 3.962 | 4.208 | 4.172 | 4.216 |
|  | $F_{99}$ | 1.485 | 1.223 | 1.366 | 1.292 |
|  | $F_{10,10}$ | 1.452 | 1.245 | 1.378 | 1.307 |
|  | $F_{89}$ | 0.976 | 0.654 | 0.773 | 0.732 |
|  | $F_{8,10}$ | -0.006 | 0.033 | 0.090 | 0.055 |
|  | $F_{9,10}$ | 0.052 | 0.011 | 0.042 | 0.024 |
| $\mathrm{B}_{1}$ | $F_{11,11}$ | 1.035 | 3.058 | 2.244 | 2.383 |
|  | $F_{12,12}$ | 1.562 | 1.283 | 1.500 | 1.379 |
|  | $F_{13,13}$ | 1.037 | 1.098 | 1.159 | 1.063 |
|  | $F_{11,12}$ | 1.014 | 0.578 | 0.654 | 0.665 |
|  | $F_{11,13}$ | 0.424 | 0.170 | 0.532 | 0.410 |
|  | $F_{12,13}$ | 0.245 | 0.119 | 0.133 | 0.135 |
| $\mathrm{B}_{2}$ | $F_{14,14}$ | 5.367 | 5.034 | 5.365 | 5.224 |
|  | $F_{15,15}$ | 6.311 5.825 | 5.785 | 6.215 | 5.992 |
|  | $F_{16,16}$ | 5.825 | 5.385 | 5.819 | 5.586 |
|  | $F_{17.17}$ | 0.849 | 0.810 | 0.815 | 0.805 |
|  | $F_{18,18}$ | 0.876 | 0.835 | 0.848 | 0.830 |
|  | $F_{14,15}$ | 0.163 | 0.123 | 0.124 | 0.135 |
|  | $F_{14,16}$ | 0.212 | 0.189 | 0.177 | 0.192 |
|  | $F_{14,17}$ | 0.200 | 0.182 | 0.159 | 0.170 |
|  | $F_{14.18}$ | 0.197 | 0.207 | 0.197 | 0.202 |
|  | $F_{15,16}$ | 0.061 | 0.039 | 0.047 | 0.051 |
|  | $F_{15,17}$ | -0.063 | -0.062 | -0.048 | -0.050 |
|  | $F_{15,18}$ | -0.126 | -0.136 | -0.121 | -0.129 |
|  | $F_{16,17}$ | -0.139 | -0.137 | -0.132 | -0.133 |
|  | $F_{16,18}$ | -0.077 | -0.084 | -0.076 | -0.076 |
|  | $F_{17,18}$ | 0.361 | 0.339 | 0.360 | 0.346 |

${ }^{a}$ Stretching force constants are in mydn $\AA^{-1}$ and bending force constants in mdyn $\AA \mathrm{rad}^{-2}$.
the planar form were the following: $R_{\mathrm{C}-\mathrm{C}}=1.457 \AA, R_{\mathrm{C}=\mathrm{C}}=$ $1.434 \AA, R_{\mathrm{C}-\mathrm{H}}=1.082 \AA$, and the angle made by the $\mathrm{C}-\mathrm{H}$ bond with the plane of the ring $=123.8^{\circ}$. A vibrational analysis confirmed this geometry to be a transition structure since one imaginary frequency was obtained ( $988 i \mathrm{~cm}^{-1}$ ).
2R CISD. Two-reference CISD (2R CISD) computations were carried out on puckered and planar bicyclobutene with analytic gradient methods newly developed at Berkeley. ${ }^{34}$ The carbon 1s orbitals were kept doubly occupied, but no virtual orbitals were frozen. Geometries were optimized for both the puckered (Table I) and planar forms ( $R_{\mathrm{C}-\mathrm{C}}=1.461 \AA, R_{\mathrm{C}=\mathrm{C}}=1.439 \AA, R_{\mathrm{C}-\mathrm{H}}$ $=1.090 \AA, \mathrm{C}-\mathrm{H}$ bond to ring-plane angle $=123.9^{\circ}$ ). Force constants of 5 (Table III), frequencies, and intensities (Table IV) were computed by taking finite differences of analytic gradients

[^4]and dipole moments. The four types of displacements required for the frequency calculation ( $\mathrm{A}_{1}, \mathrm{~A}_{2}, \mathrm{~B}_{1}$, and $\mathrm{B}_{2}$ ) gave 74576 , 145588,145767 , and 148462 configuration state functions (CSFs), respectively. Completely symmetrized internal coordinates (Table II) were displaced by $\pm 0.01 \AA$ and $\pm 0.01$ radians. All cubic contaminations were eliminated by appropriately using positive and negative displacements. CISD dipole moments were computed as expectation values rather than as derivatives with respect to an electric field. ${ }^{35}$

## Results and Discussion

Optimized Geometry. In Ta 0 le I are given the optimized geometries of bicyclobutene for various methods of calculation. However, we have determined that the previously reported STO- $3 \mathrm{G}^{23}$ and $4-31 \mathrm{G}^{24 \mathrm{c}}$ structures are not minima on their respective potential surfaces since a single imaginary frequency was obtained in the vibrational analyses with both basis sets (see Table IV). Apparently polarization functions on carbon ( $6-31 \mathrm{G}^{*}$ ) are required in order to make bicyclobutene an energy minimum. The normal mode of the $B_{1}$ imaginary frequency in both cases corresponds to a ring deformation in which only a single plane of symmetry is preserved (see below).
As seen from Table I the trends from increasing the size of the basis set and the inclusion of electron correlation are those normally expected. However, it is apparent from the MP2 geometry that the carbon-carbon double bond length is significantly overestimated ( $S=1.412 \AA$ ) when this value is compared with the other correlated values ( $S=1.375-1.385 \AA$ ). The increase in the value of this bond distance on going from the 6-31G* basis set at the SCF level to the MP2 level is in fact quite large ( 1.344 $\rightarrow 1.412 \AA$ ). While an increase in the bond length is to be expected, this increase is much larger than any we have encountered in the past. This result suggests that a one-reference method for computing electron correlation (MP2) might not be suitable for bicyclobutene (see below). All the ab initio methods do predict that bicyclobutene should have a strongly puckered structure ( $\tau=128.3-138.1^{\circ}$ ). This is in strong contrast to the MINDO/3 result ${ }^{26}$ which predicts a planar carbon skeleton for bicyclobutene.

Force Constants, Frequencies, and Intensities. Calculated force constants for the various basis sets are given in Table III for the symmetry coordinates in Table II. In all cases force constants were obtained at the optimized geometry for the basis set used. Force constants are often computed at experimental or corrected ab initio geometries. ${ }^{36}$ However we have found that this is not necessary ${ }^{37.38}$ since the pattern obtained when both $1 R$ frequencies and intensities are computed normally compares quite favorably with the experimental pattern. Computed frequencies and IR intensities (the $\mathrm{A}_{2}$ block is Raman active only) are given in Table IV. The SCF 6-31G* frequencies were obtained both numerically and analytically. The latter were computed with gaussian 82. It is reassuring to see that the largest difference between the frequencies obtained from a numerical evaluation of the second derivatives of the energy and those from analytical second derivatives is only $5 \mathrm{~cm}^{-1}$.

Examination of the normal modes led to the assignments given in Table IV. These assignments are consistent for all theoretical methods with the exception of the $\mathrm{B}_{1}$ block for $6-31 \mathrm{G}^{*} / \mathrm{MP} 2$. This discrepancy is another indication of the possible inadequacy of
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Table IV. Calculated Frequencies and IR Intensities of Bicyclobutene ${ }^{a}$

| symmetry <br> species | STO-3G | $4-31 \mathrm{G}$ | $6-31 \mathrm{G}^{*}$ <br> numerical $^{b}$ | $6-31 \mathrm{G}^{*}$ <br> analytical $^{b}$ | $6-31 \mathrm{G}^{*}$ <br> MP2 | $6-31 \mathrm{G}^{*}$ <br> TCSCF | DZP <br> TCSCF | 6-31G* <br> 2R CISD | assignment ${ }^{c}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |

${ }^{a}$ Frequencies in $\mathrm{cm}^{-1}$; relative IR intensities given in parentheses. ${ }^{b}$ See text. ${ }^{c}$ While the four hydrogens are not equivalent due to symmetry, their vibrations are strongly coupled. Scissoring, wagging, rocking, and twisting modes of the $\mathrm{CH}_{2}$ groups are described with respect to the HCH plane. ${ }^{d}$ Ring def $+\mathrm{CH}_{2}$ wag. ${ }^{e} \mathrm{CH}_{2} \operatorname{def}(\gamma) .{ }^{f} \mathrm{CH}_{2} \operatorname{def}(\phi)$.
the MP2 method for bicyclobutene. It is interesting that even the SCF $\left(6-31 G^{*}\right)$ assignments are in agreement with the other correlated results.

There are two notable differences between the $6-31 \mathrm{G}^{*}$ SCF and MP2 frequencies. The $A_{1} C=C$ stretch is shifted more than 200 wavenumbers to lower frequency, and the lowest frequency $\mathrm{B}_{1}$ absorption is shifted more than 300 wavenumbers to higher frequency by the MP2 computation. Both of these shifts are much larger than those we have observed previously when using the MP2 method. ${ }^{5,6,19}$ These frequency shifts and the large change in geometry mentioned above prompted us to pursue methods based on multireference wave functions. It is reassuring (see Table IV and Figure 2) that the two methods chosen (TCSCF and 2R CISD) gave results consistent with one another. Since it was found that bicyclobutene is likely to have significant diradical character, it is surprising that the $6-31 G^{*}$ SCF computed spectrum (when both frequencies and intensities are compared) agrees as well as it does with the two-reference results. The only major differences are in the two lower $B_{1}$ frequencies, which are too low in the SCF computation, although the SCF intensities are in reasonable agreement with those of the TCSCF and 2R CISD methods.

While there are four $\mathrm{C}-\mathrm{H}$ stretching vibrations predicted in the IR spectrum of 5 , in all cases the calculated symmetric and antisymmetric stretching vibrations of each pair of equivalent hydrogens have almost the same frequency. Therefore in the infrared spectrum of 5 one is likely to observe only two ( $\mathrm{C}-\mathrm{H}$ ) bands with each band corresponding to two closely spaced ( $\mathrm{C}-\mathrm{H}$ ) modes of $A_{1}$ and $B_{2}$ symmetry. The plotted intensity of each $C-H$ band in Figure 2 is the sum of intensities of individual components.

The $C=C$ stretching vibration ( $\mathrm{A}_{1}$ ) corresponds to a very weak band in the IR spectrum, and its position might very well be obscured by the presence of the close-lying $B_{2}$ mode associated with ring deformation (see Table IV). Bending motions of the two pairs of nonequivalent hydrogen atoms were found to be strongly coupled; however, these motions are easily interpreted as $\mathrm{CH}_{2}$ scissoring, rocking, twisting, and wagging modes by taking linear combinations of the symmetrized internal coordinates in each symmetry block (Table II) and appropriately transforming the normal mode eigenvectors.

Of note also is the very intense band $\left(\mathrm{B}_{1}\right)$ predicted to a ppear at quite low wavenumber. The unusually high intensity of this band indicates the increase of polarity in the molecule during this particular normal vibration. From the examination of the $B_{1}$ normal mode obtained, it is seen that this band corresponds to the deformation of the carbon skeleton in which displacement of the carbon atoms does produce a large change in the dipole moment. The force constant associated with this normal mode


Figure 2. Computed IR spectra of bicyclobutene (5).
( $F_{11,11}$ ) is much smaller than $F_{11}, F_{88}$, and $F_{14,14}$, which correspond to the deformations of the carbon skeleton of $A_{1}, A_{2}$, and $B_{2}$ symmetry, respectively. Distortion of the molecule along this $B_{1}$ normal mode will eventually break the two carbon-carbon bonds according to the scheme


This distortion has an imaginary frequency with the STO-3G and $4-31 \mathrm{G}$ basis sets. It is seen that as the size of the basis set is increased, the frequency of this $B_{1}$ distortion changes from imaginary to real; and inclusion of electron correlation increases the value even further. This is additional evidence that one must exercise caution in the choice of the method of calculation in

Table V. Energy of Planar Bicyclobutene ( $D_{2 h}$ ) and Barrier to Inversion of the $C_{2 v}$ Form

| molecule | method ${ }^{\text {a }}$ | energy <br> (hartree) | $\begin{gathered} \text { classical } \\ \text { barrier }^{d} \\ (\mathrm{kcal} / \mathrm{mol}) \\ \hline \end{gathered}$ |
| :---: | :---: | :---: | :---: |
| bicyclobutene ( $D_{2 h}$ ) | $\begin{aligned} & 6-31 \mathrm{G}^{*} \mathrm{SCF} / / 6-31 \mathrm{G}^{*} \\ & \mathrm{SCF} \end{aligned}$ | -153.55949 | $13.0{ }^{\text {b }}$ |
|  | $6-31 \mathrm{G}^{*} \mathrm{MP} 2 / / 6-31 \mathrm{G}^{*}$ MP2 | -154.09596 | 7.6 |
|  | DZP TCSCF//6-3IG* <br> 2R CISD | -153.61600 | 18.4 |
|  | DZP 2R CISD//6-31G* 2R CISD ${ }^{c}$ | $-154.08570$ | 14.1 |
|  | $\begin{aligned} & \text { DZP 2R CIDVD } / / 6-31 G^{*} \\ & \text { 2R CISD } \end{aligned}$ | -154.15040 | 12.5 |

${ }^{a}$ Abbreviations: $/ /=$ at the geometry of; CIDVD = Davidson-corrected CISD. See footnote $a$ of Table VI. ${ }^{b}$ Reference 24c. ${ }^{c} 56773$ CSFs. ${ }^{d}$ The following harmonic frequencies (in $\mathrm{cm}^{-1}$ ) were obtained at the $6-31 \mathrm{G}^{*}$ TCSCF level of theory for $D_{2 h}$ bicyclobutene: $3235,1738,1288,936\left(\mathrm{~A}_{\mathrm{g}}\right)$; 1314, $1064\left(\mathrm{~B}_{1 \mathrm{~g}}\right) ; 841\left(\mathrm{~B}_{2 \mathrm{~g}}\right) ; 3285,1296\left(\mathrm{~B}_{3 \mathrm{~g}}\right) ; 1120\left(\mathrm{~A}_{4}\right) ; 3288,1021,988 i$ $\left(\mathrm{B}_{1 \mathrm{u}}\right) ; 3229,1719,1598\left(\mathrm{~B}_{2 \mathrm{u}}\right)$; and $1263,454\left(\mathrm{~B}_{3 \mathrm{u}}\right)$. Thus, the $6-31 \mathrm{G}^{*}$ TCSCF zero-point correction to the barrier is $-422 \mathrm{~cm}^{-1}=-1.21 \mathrm{kcal} / \mathrm{mol}$.


Figure 3. CIDVD (Davidson-corrected CISD) energies of $\mathrm{C}_{4} \mathrm{H}_{4}$ isomers relative to that of vinylacetylene.
dealing with such highly unusual and strained systems.
Barrier to Ring Inversion of Bicyclobutene. As shown by our 6-31G* TCSCF vibrational analysis, a likely transition structure for the ring inversion of bicyclobutene is the structure with all carbon atoms in a plane ( $D_{2 h}$ ). Wiberg has computed the energy of this barrier and found a value of $19 \mathrm{kcal} / \mathrm{mol}$ with the $4-31 \mathrm{G}$ basis set and $13 \mathrm{kcal} / \mathrm{mol}$ with the $6-31 \mathrm{G}^{*}$ basis set. ${ }^{24 \mathrm{c}}$ In Table V are given current energies of the $D_{2 h}$ structure and the barrier to inversion for the various methods of calculation. From these values it is concluded that if bicyclobutene were prepared at the temperature of an argon or nitrogen matrix, ring inversion would not occur.

Relative Energies of $\mathrm{C}_{4} \mathbf{H}_{4}$ Isomers. Table VI lists the energies computed at various levels of theory for six $\mathrm{C}_{4} \mathrm{H}_{4}$ isomers. Their energies relative to that of vinylacetylene are also given in the table and depicted in Figure 3. Of the isomers considered, vinylacetylene is the most stable in all basis sets, followed by methylenecyclopropene and cyclobutadiene. The three remaining isomers, bicyclobutene, tetrahedrane, and cyclobutyne, are all predicted to be of considerably lower stability, although their ordering is seen to be dependent upon the method of calculation used. At the highest level (DZP CIDVD) bicyclobutene and tetrahedrane are both predicted to be approximately $30 \mathrm{kcal} / \mathrm{mol}$ less stable than cyclobutadiene with cyclobutyne being about $40 \mathrm{kcal} / \mathrm{mol}$ less stable than cyclobutadiene. These results suggest that the

Table VI. Energies of $\mathrm{C}_{4} \mathrm{H}_{4}$ Isomers
$\left.\begin{array}{ccc}\hline \text { molecule/method } & & \begin{array}{c}\text { relative } \\ \text { energy }\end{array} \\ \text { (hartree) }\end{array}\right)$ kcal/mol)
${ }^{a}$ Abbreviations: // = at the geometry of; CIDVD = Davidson-corrected CISD. ${ }^{39.40}$ For TCSCF cases the two-reference Davidson-like correction was computed according to the formula $\Delta E=\left(1-C_{1}{ }^{2}-\right.$ $\left.C_{2}^{2}\right)\left(E_{\mathrm{CISD}}-E_{\mathrm{TCSCF}}\right) .{ }^{b} 3-21 \mathrm{G}$ geometry: Carnegie-Mellon Quantum Chemistry Archive. ${ }^{\text {c }}$ Reference 5. ${ }^{d}$ Reference 19. ${ }^{e}$ Reference 6. ${ }^{\delta}$ Reference $21 \mathrm{a} .{ }^{8}$ These are relative energies of the potential minima. They do not include thermodynamic corrections, the largest of which is the zero-point vibrational energy (ZPVE). At the $6-31 \mathrm{G}^{*} \mathrm{SCF}$ or TC SCF level, the unscaled, harmonic ZPVE corrections to the relative energies of methylenecyclopropene, cyclobutadiene, bicyclobutene, and tetrahedrane are $-0.32,-0.42,+0.67$, and $-0.70 \mathrm{kcal} / \mathrm{mol}$, respectively.
synthesis of bicyclobutene, tetrahedrane, and cyclobutyne will need to be performed in a low-temperature matrix since even cyclobutadiene is known to be stable only in such an environment.
Comments on Bonding in Bicyclobutene. The four most important configurations in the CI wave function for planar ( $D_{2 h}$ ) bicyclobutene can be described by structures A-D. In the planar CI vector the coefficients arising from these electronic structures are $C_{1}=0.910(\mathrm{~A}) ; C_{2}=-0.192(\mathrm{~B}) ; C_{3}=-0.064$ and $C_{6}=0.036$ (D); and $C_{4}=-0.052$ (C). Hence,

while $A$ and $B$ are dominant, $C$ and $D$ nevertheless make a significant contribution. Examination of the importance of these electronic structures for bent ( $C_{2 v}$ ) bicyclobutene reveals $C_{1}=$ $0.903(\mathrm{~A}) ; C_{2}=-0.232(\mathrm{~B}) ; C_{3}=0.045$ and $C_{19}=-0.018(\mathrm{D}) ;$ and $C_{5}=-0.035(\mathrm{C})$. Thus, in the bent form A and B are
significantly more dominant over C and D than in the planar form. Hence the only antibonding orbital in bent bicyclobutene that is of critical importance can be viewed as arising from structure B. However, as the molecule is bent, the $\sigma$ and $\pi$ orbitals mix; and this antibonding orbital in fact is a $\pi^{*}-\sigma^{*}$ hybrid.

A consequence of the importance of this antibonding orbital is that bent bicyclobutene is likely to have significant diradical character, which of course will add to its chemical reactivity. For example, bicyclobutene might be expected not only to undergo Diels-Alder reactions readily (Szeimies has trapped the bicyclobutene derivative 7 with diphenylisobenzofuran) but also, because of its diradical character, it may very likely undergo Woodward-Hoffmann forbidden $[2+2]$ cycloadditions. One possibility is the dimerization


Evidence for this type of reaction has in fact been obtained for the pyramidalized alkene 9 by Borden, who has found that this molecule readily undergoes a $[2+2]$ dimerization. ${ }^{41}$


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Because of the likely diradical character of bicyclobutene, a competing reaction to the [ $2+2$ ] dimerization might very well be polymerization. Szeimies has obtained some evidence that the polymerization reaction may be important. ${ }^{22 b} \mathrm{He}$ found that while the bicyclobutene 8 can be trapped with various dienophiles, an attempt to produce its [ $2+2$ ] dimerization product 10 (no trapping agents were added) gives only a polymeric substance.


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The $\tilde{\mathbf{a}}^{3} \mathbf{B}_{1}$ State of Bicyclobutene. The presence of a low-lying $\pi^{*}$ orbital in bicyclobutene not only imparts significant diradical character to the ground electronic state but also provides for the existence of a low-lying triplet excited state ( $\sigma^{2} \pi \pi^{*}$ ) of $\mathrm{B}_{1}$ symmetry. One should consider the possibility that the chemistry exhibited by bicyclobutenes might also involve this triplet diradical state. Thus, additional calculations were undertaken to characterize the ${ }^{3} \mathrm{~B}_{1}$ state. By using the $6-31 \mathrm{G}^{*}$ basis and RHF SCF wave functions, $D_{2 h}$ and $C_{2 v}$ stationary points for the ${ }^{3} \mathrm{~B}_{1}$ state were located and characterized at Berkeley with analytic first and second energy derivative methods. ${ }^{21 b}$ Vertical and adiabatic excitation energies were then obtained at $6-31 \mathrm{G}^{*}$ CISD and Davidson-corrected CISD (CIDVD) levels of theory. The geometrical structures, vibrational frequencies, and excitation energies appear in Table VII.

The $6-31 \mathrm{G}^{*} \mathrm{SCF}$ structure ( $C_{2 \mathrm{v}}$ ) for the ${ }^{3} \mathrm{~B}_{1}$ state is even more strongly puckered than the analogous structure for the ground state ( $\tau=119.3^{\circ}$ vs. $133.5^{\circ}$ ), but the ${ }^{3} \mathrm{~B}_{1}$ SCF inversion barrier is predicted to be much smaller than the $\tilde{\mathbf{X}}^{1} \mathrm{~A}_{1}$ TCSCF barrier ( 5.4 vs. $18.3 \mathrm{kcal} / \mathrm{mol}$ ). The ${ }^{3} \mathrm{~B}_{1} \mathrm{C}=\mathrm{C}$ distance in the $C_{2 v}$ structure ( $S=1.430 \AA$ ) is $0.055 \AA$ longer than the $\tilde{\mathrm{X}}^{1} \mathrm{~A}_{1}$ TCSCF value, such a moderate lengthening being expected. However, the $S=1.758 \AA$ distance in the ${ }^{3} \mathrm{~B}_{1} D_{2 h}$ structure is over $0.3 \AA$ longer than the $\tilde{\mathbf{X}}^{1} \mathrm{~A}_{1}$ distance of $S=1.434 \AA$. Thus, it is evident from the geometrical structures and the inversion barrier that the $\mathrm{C}-\mathrm{C}$ bond remaining across the ring in the ${ }^{3} \mathrm{~B}_{1}$ electronic state is quite weak. In fact, the $D_{2 h}{ }^{3} \mathrm{~B}_{1}$ CISD wave function exhibits a relatively large $\sigma^{2} \rightarrow \sigma^{* 2} \mathrm{CI}$ coefficient ( $C_{2}=-0.098$ ). Finally, note in Table VII that the ${ }^{3} \mathrm{~B}_{1}$ state actually appears to have a $D_{2 h}$ minimum at the CISD and CIDVD levels. It is clear that the ${ }^{3} \mathrm{~B}_{1}$ CISD (or CIDVD) potential energy surface is relatively flat as the molecule puckers and the carbon-carbon distance $S$

Table VII. Theoretical Data for the $\tilde{a}^{3} \mathrm{~B}_{1}$ State of Bicyclobutene Predicted with the 6-31G* Basis Set ${ }^{a}$

${ }^{a}$ The designation $C_{2 v}$ refers to the puckered conformation (Figure 1), and $D_{2 h}$ refers to the conformation in which all carbon atoms lie in a plane. ${ }^{b}$ Bond distances in $\AA$, angles in deg, and absolute energies in hartrees. The geometrical parameters are defined in Table I (footnote b). ${ }^{c} D_{2 h}$ symmetry imposes the following constraints: $T=U, \alpha=\beta$, and $\tau=180^{\circ}$. UObtained at the optimum SCF geometry with the carbon 1 s core orbitals frozen. CIDVD $=$ Davidson-corrected CISD. Note that the $D_{2 h}$ CISD and CIDVD energies are lower than the $C_{2 v}$ values. ${ }^{2}$ Based on the $6-31 G^{*}$ TCSCF geometry for the $\tilde{X}^{1} A_{1}$ state and the $6-31 G^{*}$ SCF geometry for the $\tilde{\mathrm{a}}^{3} \mathrm{~B}_{1}$ state. The $6-31 \mathrm{G}^{*} \mathrm{TC}$ SCF, 2R CISD, and 2R CIDVD (see footnote $a$ of Table VI) energies were used for the $\bar{X}^{1} \mathrm{~A}_{1}$ state, and the corresponding one-reference values were employed for the $\tilde{a}^{3} \mathrm{~B}_{1}$ state. Zero-point vibrational energy (ZPVE) corrections were not included. ${ }^{f}$ For convenience the frequencies are listed in the $C_{2 v}$ ordering appearing in Table IV. The $D_{2 h}$ symmetry species are given in parentheses.
varies. A CISD or MCSCF geometry optimization would be necessary to establish firmly the point group of the ${ }^{3} \mathrm{~B}_{1}$ (or ${ }^{3} \mathrm{~B}_{34}$ ) minimum.

As seen in Table VII, the SCF harmonic vibrational frequency for stretching the $\mathrm{C}-\mathrm{C}$ bond length $S$ is $1461 \mathrm{~cm}^{-1}$ in the $C_{20}$ conformation of ${ }^{3} \mathrm{~B}_{1}$ bicyclobutene. This frequency is only $10 \mathrm{~cm}^{-1}$ below the $6-31 \mathrm{G}^{*}$ TCSCF value for the ground state. However, in the $D_{2 h}$ conformation this frequency is reduced to $890 \mathrm{~cm}^{-1}$, which is more typical of a bending mode in a carbon ring without
a bridge. Other comparisons between the frequencies of $\tilde{a}^{3} \mathrm{~B}_{1}$ and $\tilde{X}^{1} \mathrm{~A}_{1}$ bicyclobutene are instructive too, but the key feature of the vibrational frequencies in Table VII is that there are no imaginary frequencies for ring-breaking modes. Thus, ${ }^{3} \mathrm{~B}_{1}$ bicyclobutene is predicted to be a relative minimum on the $\mathrm{C}_{4} \mathrm{H}_{4}$ potential energy surface with either $D_{2 h}$ or $C_{2 v}$ symmetry.

The adiabatic excitation energy for the transition $\left(C_{2 v}\right) \tilde{\mathbf{X}}^{1} \mathrm{~A}_{1}$ $\rightarrow\left(C_{2 x}\right) \tilde{\mathrm{a}}^{3} \mathrm{~B}_{1}$ is $45.8 \mathrm{kcal} / \mathrm{mol}$ at the SCF level and $49.2 \mathrm{kcal} / \mathrm{mol}$ at the CISD level. The corresponding $\left(D_{2 h}\right) \tilde{\mathrm{X}}^{1} \mathrm{~A}_{1} \rightarrow\left(D_{2 h}\right) \tilde{\mathrm{a}}^{3} \mathrm{~B}_{1}$ results are 32.9 and $35.8 \mathrm{kcal} / \mathrm{mol}$, respectively. The $13-\mathrm{kcal} / \mathrm{mol}$ reduction in the latter two values is primarily due to the energy difference between the $C_{2 v}$ and $D_{2 h}$ conformations of the ground state; thus, regardless of whether the $\tilde{a}^{3} \mathrm{~B}_{1}$ state actually has a $D_{2 h}$ minimum, the ( $C_{2 v}$ ) $\tilde{\mathrm{X}}^{1} \mathrm{~A}_{1} \rightarrow \tilde{\mathrm{a}}^{3} \mathrm{~B}_{1}$ adiabatic excitation energy should be near $17500 \mathrm{~cm}^{-1}$, or $50 \mathrm{kcal} / \mathrm{mol}$. Utilizing DZ SCF geometries, ${ }^{42}$ the 6-31G* CISD $\left(D_{2 h}\right) \mathrm{N}\left(\pi^{2}\right) \rightarrow\left(D_{2 h}\right) \mathrm{T}\left(\pi \pi^{*}\right)$ adiabatic excitation energy for ethylene is $78.8 \mathrm{kcal} / \mathrm{mol}$. (The corresponding ( $D_{2 h}$ ) $\mathrm{N}\left(\pi^{2}\right) \rightarrow\left(D_{2 d}\right) \mathrm{T}\left(\pi \pi^{*}\right) \mathrm{C}_{2} \mathrm{H}_{4}$ value of 62.0 $\mathrm{kcal} / \mathrm{mol}$ is less pertinent since ${ }^{3} \mathrm{~B}_{1}$ bicyclobutene is not twisted.) Thus, while the singlet-triplet splitting in bicyclobutene is indeed smaller than that in ethylene, the data in Table VII show that the a ${ }^{3} \mathrm{~B}_{1}$ state of bicyclobutene lies over $30 \mathrm{kcal} / \mathrm{mol}$ above the ground state even at the $\tilde{\mathbf{X}}^{1} \mathrm{~A}_{1}$ transition state to inversion. The $\tilde{\mathrm{a}}^{3} \mathrm{~B}_{1}$ state should not be a factor in the chemistry of bicyclobutene unless it is photochemically populated.
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Finally, we find the $\pi^{2} \sigma \sigma^{*}$ triplet state to be $80.8 \mathrm{kcal} / \mathrm{mol}$ ( $6-31 \mathrm{G} * \mathrm{SCF}$ ) above the $\sigma^{2} \pi \pi^{*}\left({ }^{3} \mathrm{~B}_{1}\right)$ triplet state at the ${ }^{3} \mathrm{~B}_{1} D_{2 h}$ optimum geometry. However, the $\sigma \pi \pi^{*} \sigma^{*}$ quintet state is much lower in energy. At the 6-31G* SCF level, this quintet state ( ${ }^{5} \mathrm{~B}_{28}$ ) has a $D_{2 h}$ optimum geometry of $R=1.521 \AA, S=2.030 \AA, T$ $=U=1.087 \AA$, and $\alpha=\beta=125.7^{\circ}$ (as defined in Table VII). An analytic SCF second derivative calculation shows this $D_{2 h}$ stationary point to be a relative minimum. The lowest frequency ( $301 \mathrm{~cm}^{-1}$ ) corresponds to ring puckering, and a frequency of 887 $\mathrm{cm}^{-1}$ is found for stretching the $\mathrm{C}-\mathrm{C}$ distance $S$, a mode which should be considered a ring-bending mode. The ${ }^{5} \mathrm{~B}_{2 \mathrm{~g}}$ state can aptly be described as two triplet methylene units high-spin coupled across a four-carbon ring. The ${ }^{5} \mathrm{~B}_{2 \mathrm{~g}}$ optimum SCF energy ( -153.54177 ) is only $3.6 \mathrm{kcal} / \mathrm{mol}$ above the optimum $\left(C_{2 v}\right)^{3} \mathrm{~B}_{1}$ energy, but, as one would expect, the inclusion of electron correlation increases this energy difference to $27.2 \mathrm{kcal} / \mathrm{mol}$ [ $E$ (CISD) $=-153.94805$ ], giving a CISD adiabatic excitation energy of $76.4 \mathrm{kcal} / \mathrm{mol}$ for the $\overline{\mathrm{X}}^{1} \mathrm{~A}_{1} \rightarrow{ }^{5} \mathrm{~B}_{2 \mathrm{~g}}$ transition.

Acknowledgment. The research performed at Berkeley was supported by the U.S. National Science Foundation, Grant No. CHE-8218785. This material is also based upon work supported under a National Science Foundation Graduate Fellowship held from 1983 to 1986 by W.D.A. The computations done at Vanderbilt were supported in part by the U. S. National Science Foundation, Grant No. CHE-8605951. We are also grateful to a referee for suggesting the calculations on the triplet state of bicyclobutene.

Registry No. 1, 1120-53-2; 2, 157-39-1; 3, 1120-53-2; 5, 58208-49-4; vinylacetylene, 689-97-4.

# Non-Kekulé Acenes. The Dimethylenepolycyclobutadienes, a New Class of $(4 n+2)$ Alternant Hydrocarbons 

Julianto Pranata and Dennis A. Dougherty*1<br>Contribution No. 7443 from the Arnold and Mabel Beckman Laboratory of Chemical Synthesis, California Institute of Technology, Pasadena, California 91125. Received July 17, 1986


#### Abstract

The dimethylenepolycyclobutadienes ( $\mathbf{3}_{n}$ ) are the non-Kekule analogies of the classical acenes. Application of a variety of theoretical methods reveals several novel features of such structures. Most interesting is the emergence of a parity rule. When $n$ is even, $3_{n}$ is predicted to be a singlet, with $n$ disjoint NBMO's. When $n$ is odd, theory predicts a triplet ground state with $(n+1)$ NBMO's that are not fully disjoint.


Interest in new organic materials with unusual optical, magnetic, and electronic properties continues to grow. Polyacetylene (1) provides a powerful paradigm for the development of such structures. One starts with a simple monomer with a relatively large HOMO-LUMO energy gap, and builds up highly extended, conjugated $\pi$ systems. As the chain grows, the HOMO-LUMO energy gap decreases, and when this gap becomes small enough, novel properties must emerge. This approach has led to the development of many new materials such as poly ( $p$-phenylene), poly( $p$-phenylene sulfide), polythiophene, etc. Another related example is provided by the classical acenes (2) (benzene, naphthalene, anthracene, ...). The smaller acenes are, of course, well-known and extensively studied. Recent theoretical and experimental work on larger acenes with $n>7$ suggests that such structures could have very intriguing properties. ${ }^{2}$


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(1) Fellow of the Alfred P. Sloan Foundation, 1983-1985; Camille and Henry Dreyfus Teacher-Scholar, 1984-1989.

An alternative strategy for building novel structures would be to start with a monomer that has essentially no HOMO-LUMO gap. With this approach, one would expect that the onset of unusual properties would occur for a "polymer" of much shorter chain length. Non-Kekulé molecules provide attractive candidates for such a monomer. A wide variety of non-Kekulé structures has been prepared in recent years, ${ }^{3}$ including some that are remarkably stable. ${ }^{36}$ Such structures can be either paramagnetic

[^5]
[^0]:    ${ }^{7}$ Vanderbilt University.
    ¥ University of California.
    ${ }^{\S}$ NSF Predoctoral Fellow.
    ${ }^{\perp}$ Permanent address: Institute of Inorganic Chemistry, Technical University of Wrocław, Wrocław, Poland.

[^1]:    ${ }^{a}$ Bond distances in $\AA$, angles in deg. ${ }^{b}$ As defined in Figure 1, except $\alpha$ is the angle made by a $\mathrm{C}-\mathrm{H}$ bond of length $T$ and the bisector of the three-membered ring and $\beta$ is the angle made by a $\mathrm{C}-\mathrm{H}$ bond of length $U$ and the same bisector. ${ }^{c}$ Reference 26. ${ }^{d}$ Reference 23. ${ }^{e}$ These in fact do not correspond to minima (see text). fReference 24 c . ${ }^{8}$ This work. ${ }^{h}$ This value is in good agreement with that reported by Wiberg (ref 24 c ).

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